

M2 JAN 06

a) $KE_{lost} = \frac{1}{2}mu^2 = \frac{1}{2}(3)(8)^2 = \underline{96J}$

b) $KE_{lost} = Wd \text{ against friction}$

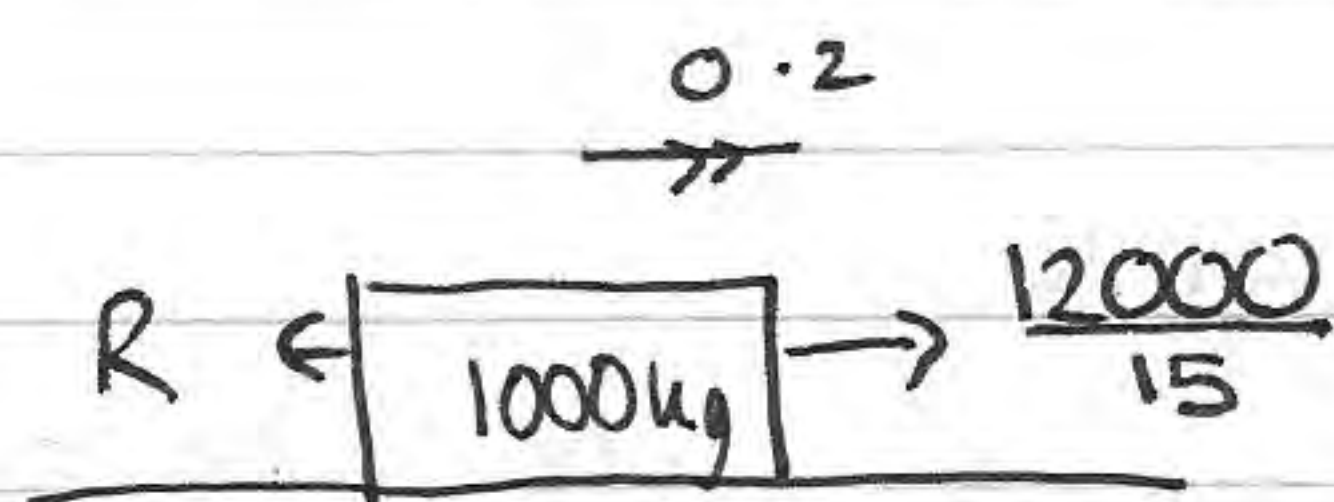
$$\Rightarrow 96 = f_{max} \times 12 \Rightarrow \mu \times NR = 8 \Rightarrow \mu = \frac{8}{3g} = 0.27(24)$$

2) $vel = \frac{dr}{dt} = (2t+4)i + (3-3t^2)j$

$t=3, v = 10i - 24j \Rightarrow \text{speed} = \sqrt{10^2 + 24^2} = \underline{13 \text{ ms}^{-1}}$

b) Initial momentum = $mu = 0.4(10i - 24j) = 4i - 9.6j$
 $+ \text{Impulse} = 8i - 12j$
 $= \text{final Mom} = MV = 12i - 21.6j$
 $\div 0.4 \quad v = \underline{30i - 54j}$

3)

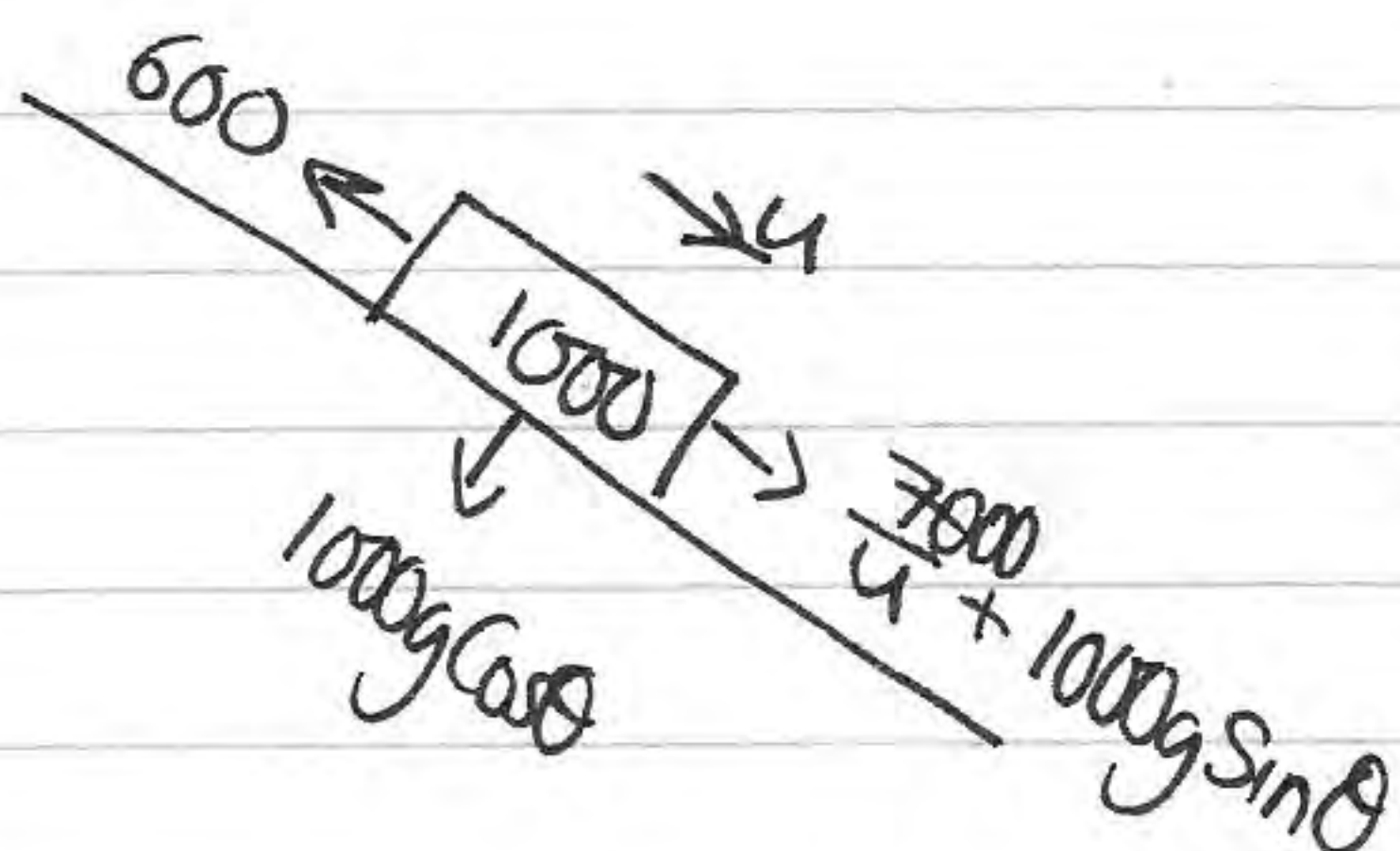


$$\vec{Rf} = ma$$

$$\Rightarrow \frac{12000}{15} - R = 1000 \times 0.2$$

$$\Rightarrow 800 - R = 200 \Rightarrow R = 600 \text{ N} \neq$$

b)

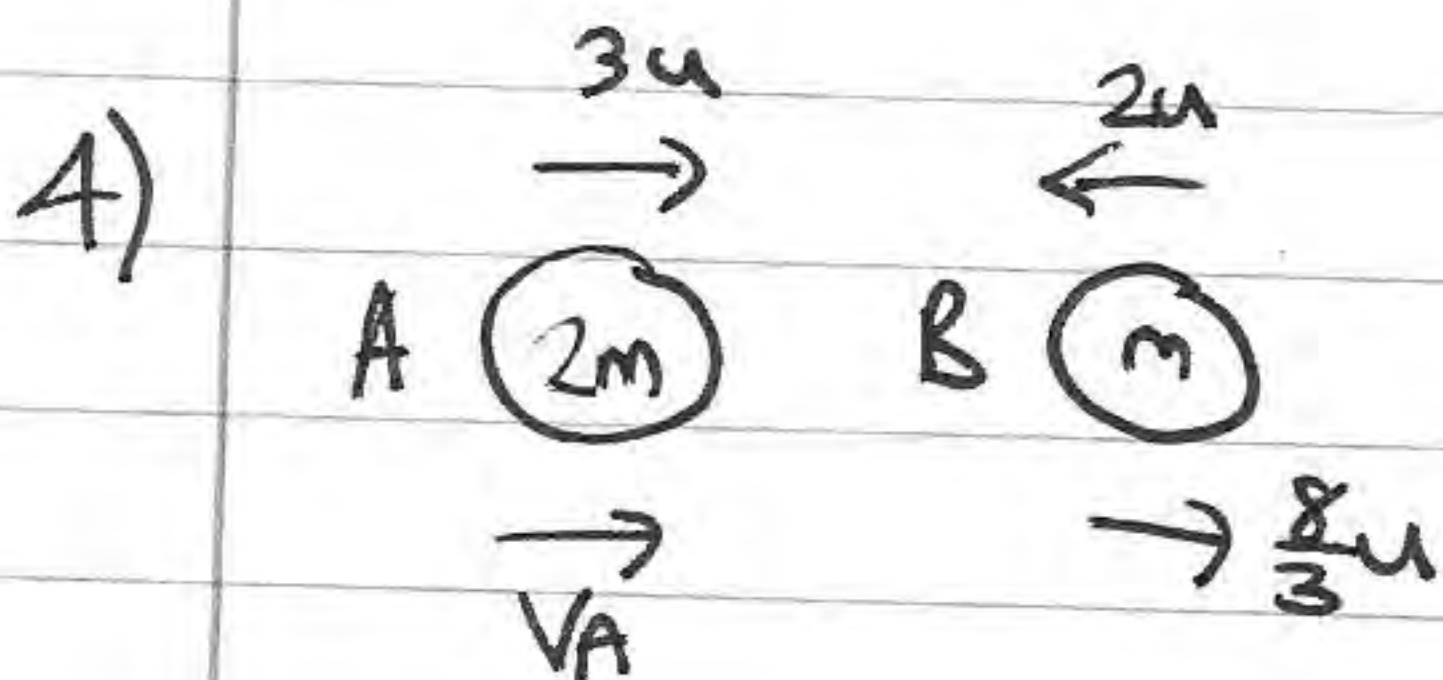


$$Rf \downarrow = 0$$

$$\Rightarrow \frac{7000}{4} + 1000g \times \frac{1}{40} = 600$$

$$\Rightarrow \frac{7000}{4} = 600 - 25g$$

$$\Rightarrow u = \frac{7000}{600 - 25g} \Rightarrow u = \underline{19.7 \text{ ms}^{-1}} \quad (3sf)$$



$$\text{CLM} \Rightarrow 2m(3u) + m(-2u) = 2m(v_A) + m\left(\frac{8}{3}u\right)$$

$$\Rightarrow 6mu - 2mu = 2mv_A + \frac{8}{3}mu$$

$$\Rightarrow \frac{4}{3}u = 2v_A \Rightarrow v_A = \frac{2}{3}u$$

$$e = \frac{\text{Sep}}{\text{app}} = \frac{2u}{5u} \Rightarrow e = \frac{2}{5}$$

b) total KE before = $\frac{1}{2}(2m)(3u)^2 + \frac{1}{2}m(2u)^2 = 11u^2$

total KE after = $\frac{1}{2}(2m)\left(\frac{2}{3}u\right)^2 + \frac{1}{2}m\left(\frac{8}{3}u\right)^2 = \frac{4}{9}u^2 + \frac{32}{9}u^2 = 4u^2$

KE lost = $11u^2 - 4u^2 = \underline{7u^2}$

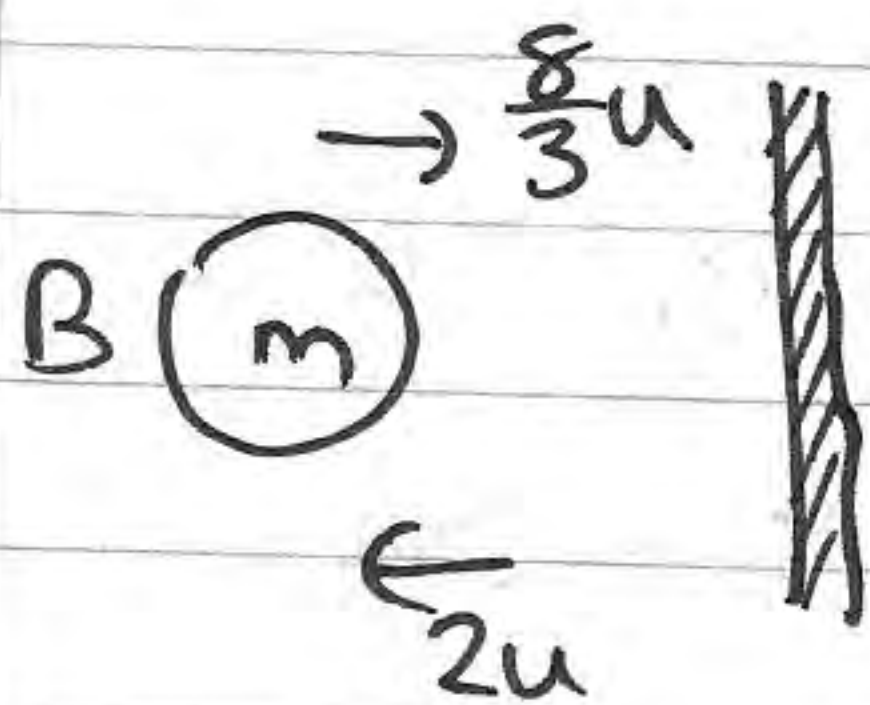
3c) Initial mom = $m\left(\frac{8}{3}u\right) = \frac{8}{3}mu$

\pm Impulse = $\frac{14}{3}mu$ (must be -)

final mom


$$= -\frac{6}{3}mu = -2mu$$

$$\Rightarrow mv = -2mu \Rightarrow v = -2u$$



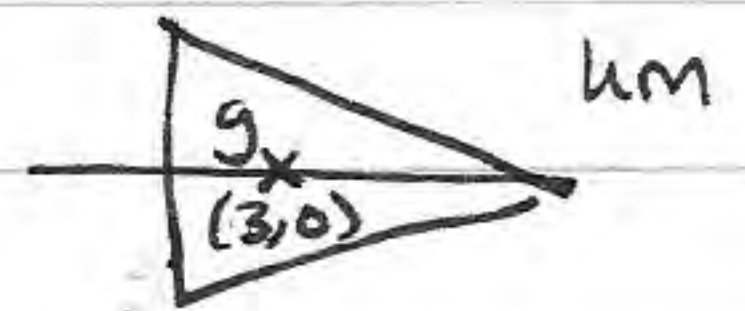
$$e = \frac{\text{Sep}}{\text{app}} = \frac{2u}{\frac{8}{3}u} = \frac{6}{8}$$

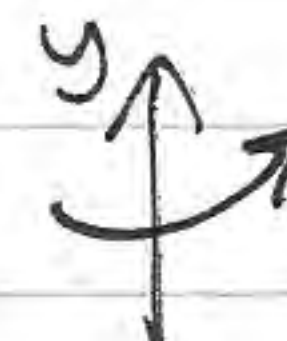
$$\Rightarrow e = \frac{3}{4}$$

5)  $4mg \times 0 + 2mg \times 0 + 6mg \times 9 = 12mg \bar{x} \Rightarrow \bar{x} = \frac{54}{12}$
 $\bar{x} = 4.5$

$\rightarrow x: 2mg \times 4 + 4mg \times 4 + 6mg \times 0 = 12mg \bar{y}$

$\bar{y} = \frac{8}{12} = \frac{2}{3} \quad (4.5, \frac{2}{3})$



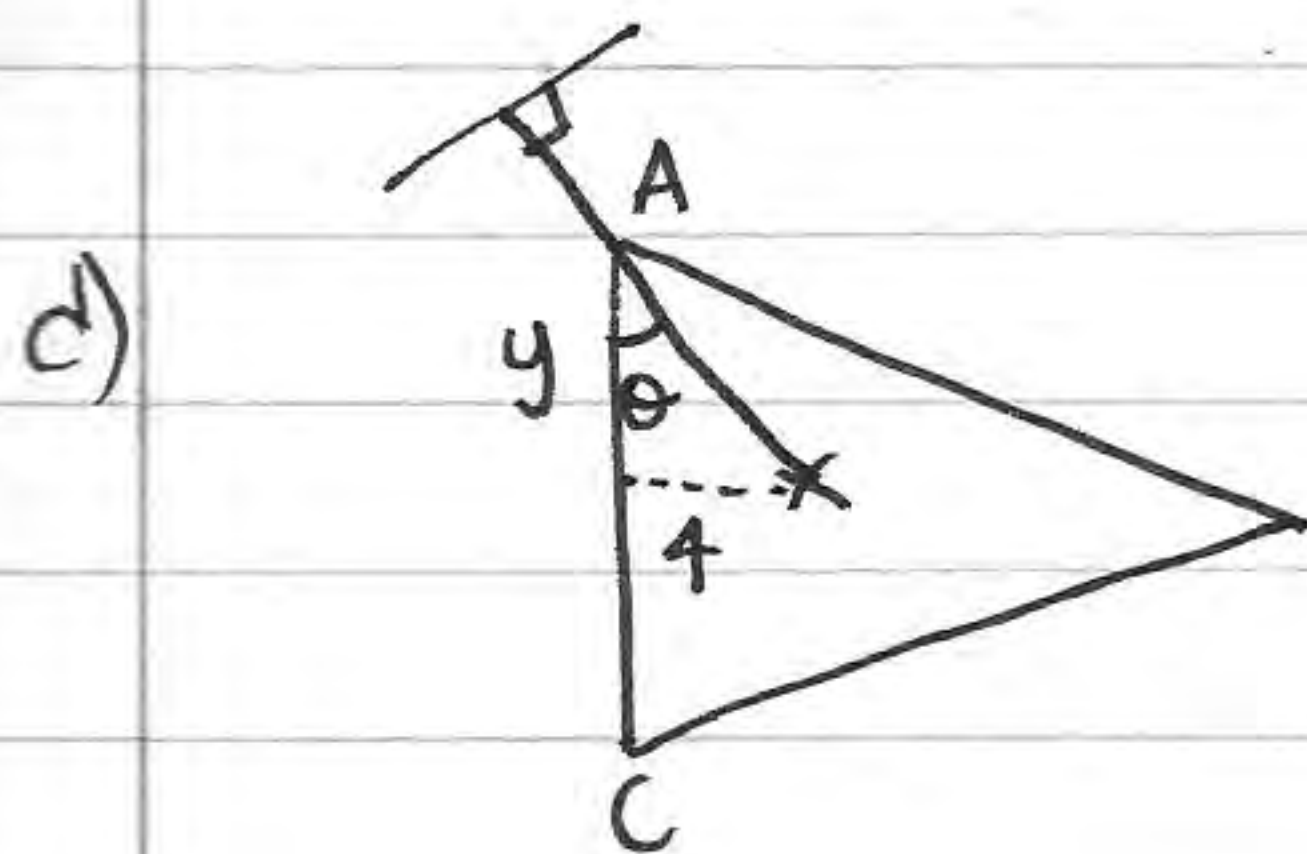
b)  $12mg \times 4.5 + 4mg \times 3 = (12+4)mg \times 4$

$\Rightarrow 54 + 3k = 4(12+4) \Rightarrow 54 + 3u = 48 + 4u$

$\Rightarrow \underline{u = 6} \#$

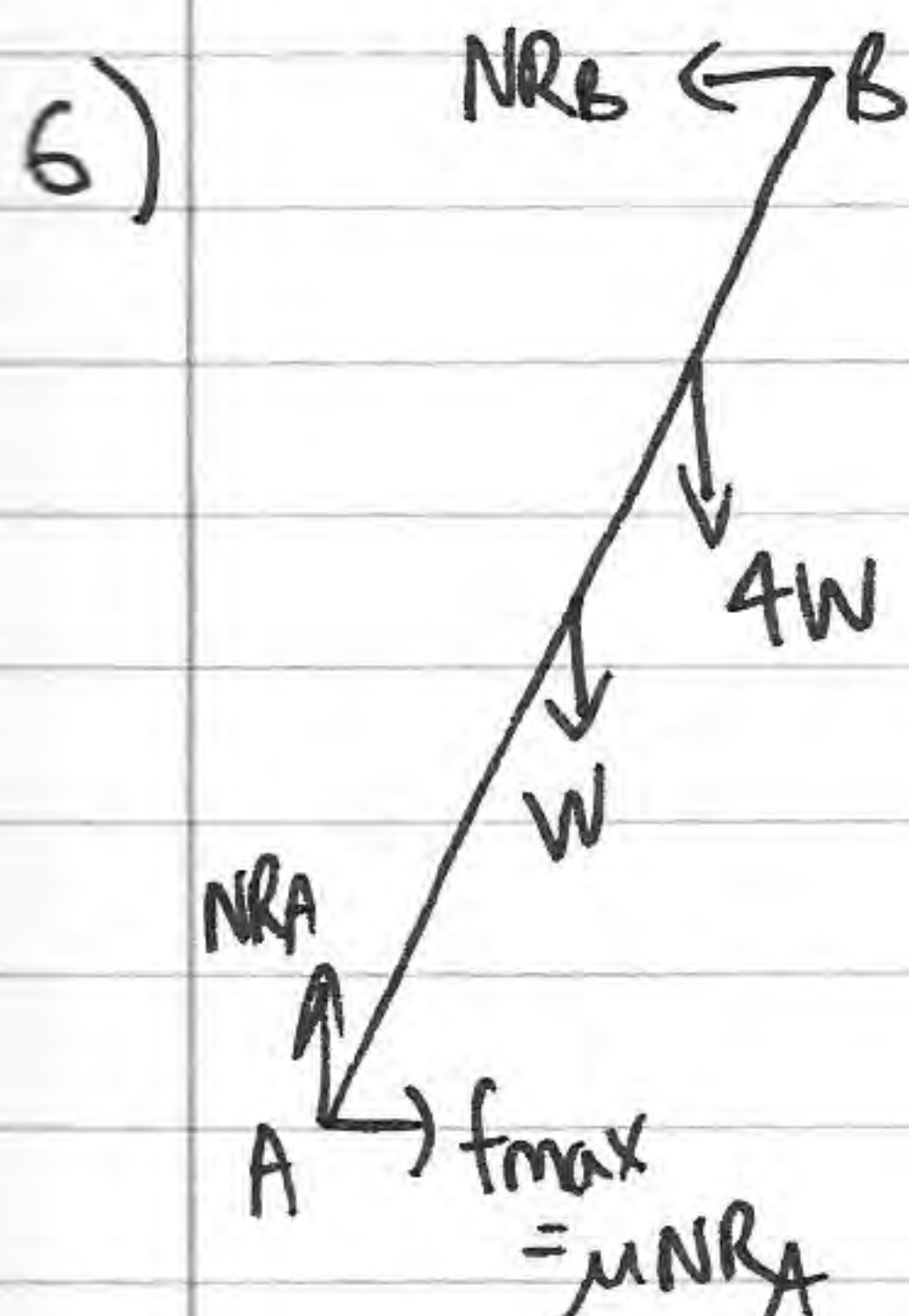
c) $\rightarrow x: 12mg \times \frac{2}{3} + 4mg \times 0 = (12+4)mg \times \lambda$

$\Rightarrow 8 = (12+4)\lambda \Rightarrow \lambda = \frac{8}{16} = \frac{1}{2}$



$y = 4 - \frac{4}{9}$

$\Rightarrow \theta = \tan^{-1}\left(\frac{4}{4 - \frac{4}{9}}\right) \Rightarrow \theta = \tan^{-1}\left(\frac{9}{8}\right) = \underline{48.4^\circ}$



$\tan \theta = \frac{2}{1} \quad \sqrt{5} \quad \sin \theta = \frac{2}{\sqrt{5}}$
 $\cos \theta = \frac{1}{\sqrt{5}}$

$R_f \uparrow = 0 \Rightarrow N_{RA} = 5W$

$\vec{R}_f = 0 \quad f_{\max} = N_{RB} \Rightarrow \mu N_{RA} = N_{RB} \Rightarrow \mu = \frac{N_{RB}}{5W}$

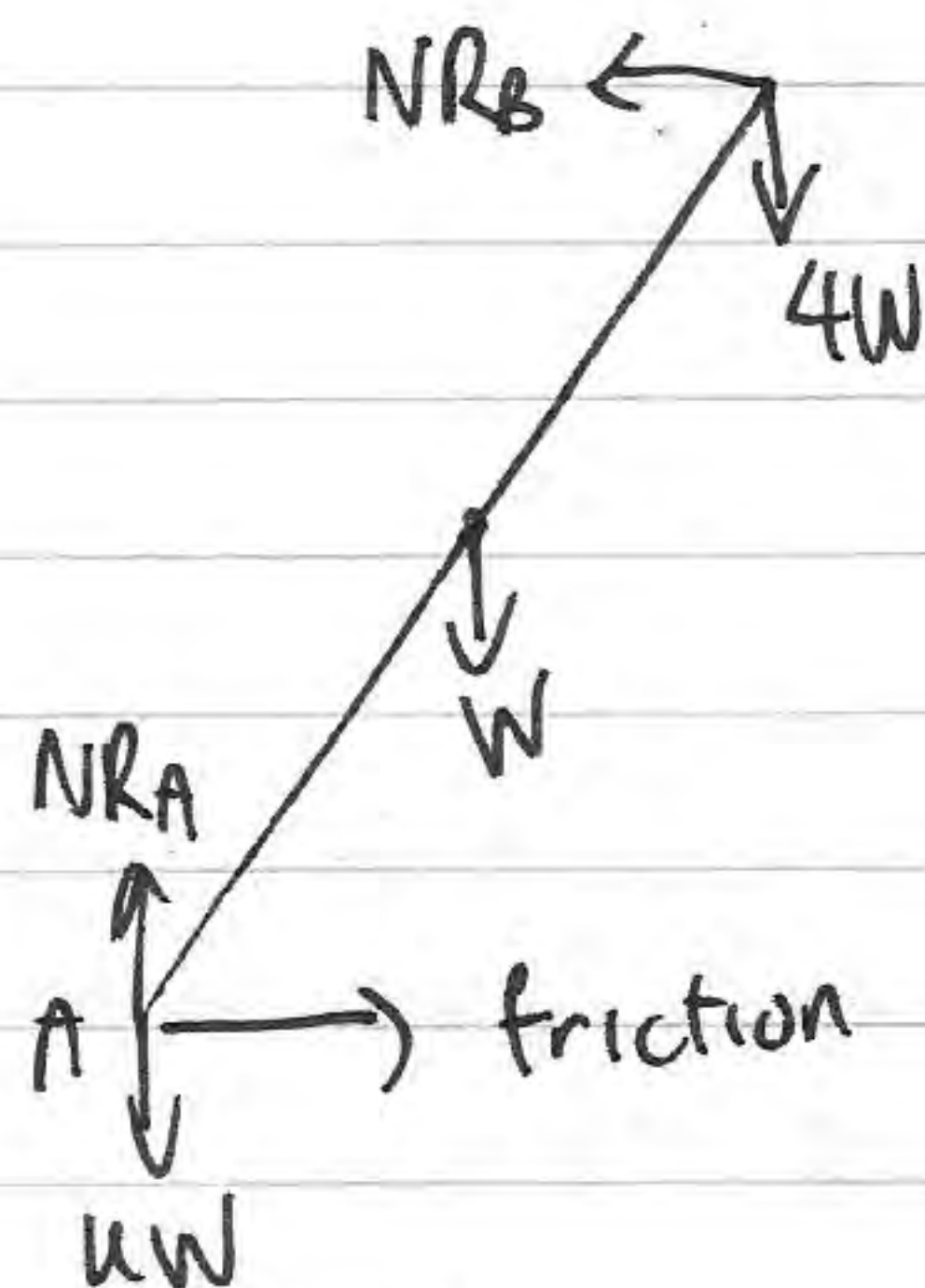
A2 $W \times 2 \times \left(\frac{1}{\sqrt{5}}\right) + 4W \times 3 \times \left(\frac{1}{\sqrt{5}}\right) = N_{RB} \times 4 \times \left(\frac{2}{\sqrt{5}}\right)$

$2W + 12W = 8N_{RB}$

$N_{RB} = \underline{\underline{\frac{14}{8}W}}$

$$\therefore \mu = \frac{\frac{14}{8}W}{5W} = \frac{14}{40} = \frac{7}{20} \#$$

b)



$$R_f \uparrow = 0 \Rightarrow N_A = (5+k)W$$

$$\vec{R}_t = 0 \Rightarrow \text{friction} = N_B$$

$$A \curvearrowright W \times 2a\left(\frac{1}{\sqrt{5}}\right) + 4W \times 4a\left(\frac{1}{\sqrt{5}}\right) = N_B \times 4a\left(\frac{2}{\sqrt{5}}\right)$$

$$\Rightarrow 2W + 16W = 8N_B \Rightarrow N_B = \frac{9}{4}W$$

$$f_{\max} = \mu N_A = \frac{7}{20}(5+k)W \quad \text{friction} = N_B = \frac{9}{4}W$$

$$\text{friction} \leq f_{\max} \Rightarrow \frac{9}{4}W \leq \frac{7}{20}(5+k)W$$

$$\Rightarrow \frac{45}{7} \leq 5+k \Rightarrow k \geq \frac{10}{7}$$

7) \vec{H} $v_{el} = 11 \cos 30$ $\text{dist} = 10 \Rightarrow t = \frac{10}{11 \frac{\sqrt{3}}{2}} = \underline{1.05}$

b) $\vec{V} \uparrow$ $u \uparrow = 11 \sin 30 = 5.5$ $a \uparrow = -9.8$ $t = \frac{20\sqrt{3}}{33}$

$$S = ut + \frac{1}{2}at^2$$

$$S = 5.5\left(\frac{20\sqrt{3}}{33}\right) - 4.9\left(\frac{20\sqrt{3}}{33}\right)^2$$

$$S = 0.374 \dots \text{ above A}$$

$$\Rightarrow C = 1 - 0.374 \dots \text{ below T}$$

$$\therefore C \text{ is } 0.63 \text{ m below T}$$

c) $u \uparrow = V \sin 30 = \frac{1}{2}V$ $a = -9.8$ $S = 1 \text{ (above A)}$

\vec{H} $v_{el} = V \cos 30$ $x = 10$

$$\Rightarrow t = \frac{10}{V \frac{\sqrt{3}}{2}} = \frac{20\sqrt{3}}{3V}$$

$$\Rightarrow 1 = \left(\frac{1}{2}V\right)\left(\frac{20\sqrt{3}}{3V}\right) - 4.9\left(\frac{20\sqrt{3}}{3V}\right)^2$$

$$\Rightarrow 1 - \frac{10\sqrt{3}}{3} = \frac{1960}{3v^2}$$

$$\Rightarrow (3 - 10\sqrt{3})v^2 = 1960 \quad \Rightarrow v = \sqrt{\frac{1960}{3 - 10\sqrt{3}}}$$

$$\underline{v = 11.7 \text{ ms}^{-1} \text{ (3sf)}}$$

- d) we have ignored wind, air resistance, spin. we have also considered the ball to be a particle, so v could be increased and decreased but still hit the target as the ball might hit the target at the top or bottom of the ball.