## C2 Trigonometry Homework 1

## Section A

1. The diagram shows a triangle $A B C$.


The lengths of $A C$ and $B C$ are 5 cm and 4.8 cm respectively.
The size of the angle $B C A$ is $30^{\circ}$.
(a) Calculate the area of the triangle $A B C$.
(b) Calculate the length of $A B$, giving your answer to three significant figures.
2. The diagram shows a sector $O A B$ of a circle with centre $O$.


The radius of the circle is 6 cm and the angle $A O B$ is 1.2 radians.
(a) Find the area of the sector $O A B$.
(b) Find the perimeter of the sector $O A B$.

## Section B

3. The diagram shows a sector $O A B$ of a circle with centre $O$ and radius $r \mathrm{~cm}$.


The angle $A O B$ is 1.5 radians. The perimeter of the sector is 56 cm .
(a) Show that $r=16$.
(b) Find the area of the sector.
4. The diagram shows a triangle


The lengths of $A C$ and $B C$ are 4.8 cm and 12 cm respectively.
The size of the angle $B A C$ is $100^{\circ}$.
(a) Show that angle $A B C=23.2^{\circ}$, correct to the nearest $0.1^{\circ}$.
(b) Calculate the area of triangle $A B C$, giving your answer in $\mathrm{cm}^{2}$ to three significant figures.
5. The diagram shows a triangle $A B C$ and the $\operatorname{arc} A B$ of a circle whose centre is $C$ and whose radius is 24 cm .


The length of the side $A B$ of the triangle is 32 cm . The size of the angle $A C B$ is $\theta$ radians.
(a) Show that $\theta=1.46$ correct to three significant figures.
(b) Calculate the length of the $\operatorname{arc} A B$ to the nearest cm .
(c) (i) Calculate the area of the sector $A B C$ to the nearest $\mathrm{cm}^{2}$.
(ii) Hence calculate the area of the shaded segment to the nearest $\mathrm{cm}^{2}$.
6. The triangle $A B C$, shown in the diagram, is such that $A C=8 \mathrm{~cm}, C B=12 \mathrm{~cm}$ and angle $A C B=$ $\theta$ radians.


The area of triangle $A B C=20 \mathrm{~cm}^{2}$.
(a) Show that $\theta=0.430$ correct to three significant figures.
(b) Use the cosine rule to calculate the length of $A B$, giving your answer to two significant figures.
(c) The point $D$ lies on $C B$ such that $A D$ is an arc of a circle centre $C$ and radius 8 cm . The region bounded by the arc $A D$ and the straight lines $D B$ and $A B$ is shaded in the diagram.


Calculate, to two significant figures:
(i) the length of the arc $A D$;
(ii) the area of the shaded region.

