Question

Show by a suitable algebraic method that

$$40^2 - 39^2 + 38^2 - 37^2 + \dots + 2^2 - 1^2 = 820$$
.

proof