

Question

The function with equation $y = f(x)$ has smooth first and second derivatives.

Show that

$$\frac{d^2y}{dx^2} + \left(\frac{dy}{dx}\right)^3 \frac{d^2x}{dy^2} = 0$$