Question   non calculator

By using trigonometric identities, show that

$$\int_{\frac{\pi}{8}}^{\frac{\pi}{4}} \frac{\sin^6 x + \cos^6 x}{\sin^2 x \cos^2 x}\, dx = \tfrac{1}{8}\left(16 - 3\pi\right).$$