Question

By using trigonometric identities, show that

$$\int_0^{\frac{\pi}{4}} \sin^4 x + \cos^4 x \ dx = \frac{3\pi}{16}.$$