Question

Find an exact simplified value for

$$\int_{\sqrt{e}}^{e} \ln(\ln x) + \frac{1}{(\ln x)^2}\ dx\,.$$