

11. Resolving radially for motion in circle

$$mg \cos \theta - R = \frac{mv^2}{r}$$

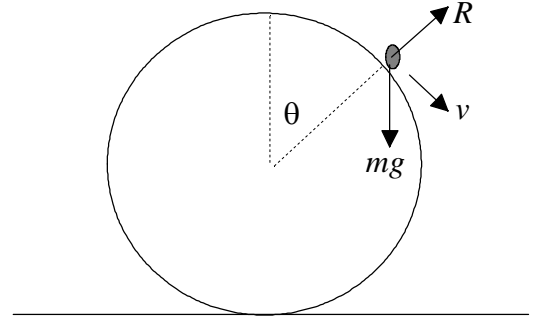
By conservation of energy

$$\frac{1}{2}mv^2 = mgr(1 - \cos \theta)$$

$$\text{so } mg \cos \theta - R = 2mg(1 - \cos \theta)$$

$$\Rightarrow R = mg(3 \cos \theta - 2)$$

Particle loses contact when $R = 0$ i.e. $\theta = \arccos \frac{2}{3}$
which is the angle of the velocity to the horizontal.



From start particle now falls a distance $2r$ so loss of potential energy is $2mgr$

horizontal component of velocity is $v \cos \theta = \frac{2v}{3}$ so if vertical component is V then gain in kinetic energy = $\frac{1}{2}m\left(\frac{4v^2}{9} + V^2\right)$ and $v^2 = 2gr(1 - \cos \theta) = \frac{2}{3}gr$

$$\text{hence, } \frac{4v^2}{9} + V^2 = 4gr \Rightarrow V^2 = 4\left(gr - \frac{v^2}{9}\right) \text{ so } V^2 = 4gr\left(1 - \frac{4}{81}\right) = \frac{308gr}{81}$$

so vertical component of momentum at floor is $\frac{308mgr}{81}$