

1

An experiment was carried out to investigate the effect of incubation temperature and concentration of bacterial inoculum on measurement of log(m-prime) which is the log-concentration of an antibiotic at which the edge of a zone of inhibition of the bacteria on an agar plate occurs. The recommended method uses a temperature of 30°C and an initial inoculum of bacteria of 10^5 c.f.u/ml.

The experiment used three temperatures and four inoculum levels and was replicated three times.

For MINITAB, temperatures are coded 1,2 & 3 and the initial inocula are coded 1,2,3 & 4.

The calculated values of log ('m-prime') and an ANOVA using Minitab were as follows:

Inoculum	Temperature °C								
	25			30			35		
0.5×10^5	2.18	2.42	2.37	1.40	1.65	1.36	1.90	2.00	2.20
1.0×10^5	1.45	1.50	1.55	1.20	1.20	2.00	1.50	1.80	1.70
2.0×10^5	1.55	1.65	1.60	1.60	1.55	1.45	1.00	1.60	1.30
4.0×10^5	1.40	1.40	1.50	1.55	1.65	1.70	1.40	1.30	1.60

Analysis of Variance (Balanced Designs) with some values replaced by #

Analysis of Variance for log(mprime)

Source	DF	SS	MS	F	P
temp	#	0.21391	0.10695	2.96	0.071
dosage	#	1.29692	0.43231	11.95	0.000
temp*dosage	#	1.21349	0.20225	5.59	#
Error	#	0.86813	0.03617		
Total	#	3.59246			

Table of means

Means

temp	N	log(mprime)
1	12	1.7142
2	12	1.5258
3	12	1.6083

innoc	N	log(mprime)
1	9	1.9422
2	9	1.5444
3	9	1.4778
4	9	1.5000

pto...

temp	innoc	N	log(mprime)
1	1	3	2.3233
1	2	3	1.5000
1	3	3	1.6000
1	4	3	1.4333
2	1	3	1.4700
2	2	3	1.4667
2	3	3	1.5333
2	4	3	1.6333
3	1	3	2.0333
3	2	3	1.6667
3	3	3	1.3000
3	4	3	1.4333

- (i) Using the analysis of variance table write out a table listing the sources as given above and completing the **column labelled DF** in the printout above.
(Do not write out all the other figures!)
- (ii) The p-value for the interaction 'temp*dosage' has been removed. Test using statistical tables whether or not there is an interaction between temperature and inoculum level.
- (iii) Re-write the table of means, properly labelled in a manner suitable for publication in a scientific journal.
- (iv) Sketch a suitable response plot.
- (v) Calculate the Least Significant Difference for comparing the means in your response plot and use it to explain the apparent pattern of response to temperature changes for each dosage.

2

An experiment was carried out to investigate the retention of ascorbic acid in a particular type of beans under storage conditions. Three storage temperatures -10°C , -20°C and -30°C and four storage times 2, 4, 6 and 8 weeks were compared. A three by four factorial design was used with each treatment replicated 3 times.

The following ANOVA table was obtained from MINITAB with its associated tables of means. Some figures in the ANOVA have been replaced by asterisks.

ANOVA

Factor	Type	Levels	Values			
Temp	fixed	3	1	2	3	
Storage	fixed	4	1	2	3	4

ANOVA for ascorbic acid

Source	df	SS	MS	F	p
Temp	*	334.389	167.19	236.04	0.000
Storage	*	40.258	13.51	19.08	0.000
Interaction	*	34.056	***	***	
Error	*	17.000	0.708		
Total	*	425.927			

Means for temp

1	15.325
2	13.825
3	8.225
ALL	12.458

Means for Storage

1	13.767
2	13.100
3	12.000
4	10.967
ALL	12.458

Means for interaction

Temp	Storage	Mean
1	1	15.000
1	2	15.700
1	3	15.300
1	4	15.300
2	1	15.000
2	2	14.300
2	3	13.700
2	4	12.300
3	1	11.300
3	2	9.300
3	3	7.000
3	4	5.300

- Complete the columns in the ANOVA table for the degrees of freedom, mean squares and F-values.
- Test whether there is any evidence of interaction between the temperature and the duration of storage.
- Use the computer output from above to complete the following table giving the figures correct to 1 d.p.

Storage	Temperature			Mean
	-10°C	-20°C	-30°C	

2 weeks

4 weeks

6 weeks

8 weeks

Mean

- (iv) Draw a response plot to illustrate the possible interaction.
- (v) Calculate a suitable Least Significant Difference for comparing the appropriate means and use it to explain what conclusions can be drawn from the table.

Nitrogen dioxide is an air pollutant caused in part by traffic. A study of its effect on lung function tested serum fluorescence in mice exposed to 0.5ppm NO₂ for 10, 12 and 14 days compared with control mice whose serum fluorescence was also measured at 10, 12 and 14 days. Thirty-six mice were used, each being tested once. High values indicate greater lung damage.

	Serum fluorescence								
	10 days			12 days			14 days		
Control group	143	169	95	179	160	87	76	40	119
	111	132	150	115	171	146	72	163	78
Exposed to NO ₂	152	83	91	141	132	201	149	104	125
	86	150	108	242	209	114	147	200	178

An analysis of variance is given below:

Analysis of Variance for serum-fluorescence

Source	DF	SS	MS	F	P
Exposure	1	4579	4579	3.17	0.085
Time	2	10600	5300	3.67	0.037
Exposure*time	2	10062	5031	3.48	0.044
Error	30	43312	1444		
Total	35	8553			

- The above is a factorial experiment. What are the two factors and how many levels has each? How many replicates are there?
- Calculate the mean for each of the six treatments and draw a response plot. Does this suggest that there is interaction between the two factors?
- Using the analysis of variance, carry out a significance test to determine whether there is evidence of interaction.
- Calculate a suitable Least Significant Difference (LSD) to test for differences among the six treatment means calculated for (b) and explain which differences are significant.
- The above data are genuine. There appears to be something radically wrong. What is it?

4

A biologist carried out an experiment to explore the strength of different lures in attracting spruce moths in relation to the position of the lures on the tree. He placed traps at four different positions in the tree: ground, lower branches, middle branches and top branches with three types of lure: chemical, scent and sugar. He counted the number of spruce moths found in each trap after 48 hours. The results from the experiment are given below.

Rows: Location Columns: Lure

	Chemical					Scent					Sugar				
Ground	22	25	14	16	19	17	12	13	19	14	18	27	15	29	16
Lower	35	39	41	31	34	44	21	38	32	9	22	17	21	29	27
Middle	37	40	18	28	36	39	12	42	25	21	16	28	14	17	12
Top	32	29	16	18	20	28	19	32	15	13	35	22	33	21	17

The data were analysed using analysis of variance. The computer output of this analysis is below. Some of the numbers have been replaced by asterisks.

Source	DF	SS	MS	F	P
Location	*	1169.4	389.8	7.27	0.000
Lure	*	327.0	163.5	3.05	0.057
Interaction	*	809.0	134.8	*	*
Error	*	2573.6	53.6		
Total	59	4879.0			

Treatment means

	Chemical	Scent	Sugar	All
Ground	20.0	15.5	22.6	19.8
Lower	36.4	34.7	24.0	32.6
Middle	33.8	32.3	19.2	30.0
Top	24.8	24.0	27.6	25.5
All	30.3	28.7	23.8	27.8

- What is the name for the experimental design used in the above study? What are the two factors? What is the number of levels for each factor? How many different treatments are there? What is the number of replicates for each treatment? What is the total number of observations?
- Replace the asterisks in the columns with the appropriate values for the degrees of freedom, mean square and F-value in the Minitab ANOVA output above.
- Draw a response plot with the 12 treatment means in the last table above. Does the response plot suggest that there is an interaction between Location and Lure?
- Using the ANOVA output in the first table above, carry out a significance test to determine whether there is any evidence of interaction between Location and Lure.
- Calculate a suitable Least Significant Difference (LSD) to test for differences among the 12 treatment means in the last table above. Explain which differences are significant and what conclusions could be drawn from the experiment.

The car company Ectel has developed a new car filter that reduces pollution from exhaust gases. However, it is very important that such filters do not increase noise pollution by reducing gas pollution. Therefore, the noise level (decibels) for the new Ectel filter was compared with a standard filter for three different sizes of vehicle (small, medium and large). The data are presented in the table below.

Noise level reading (decibels) according to type of silencer and vehicle size

Type of silencer	Standard	Vehicle size								
		Small			Medium			Large		
		810	820	820	840	840	845	785	790	785
Type of silencer	Ectel filter	835	835	835	845	855	850	760	760	770
		820	820	820	820	820	825	775	775	775
		825	825	825	815	825	825	770	760	765

- a) The data in the above table are based on a factorial design with two factors. State the response variable, the factors, the levels for each factor, the number of replications for each treatment combination and the total number of observations.
- b) Replace the asterisks in the table below with the appropriate values for the degrees of freedom and the F-value for interaction.

Analysis of variance for Noise level reading (decibels)

Source	DF	SS	MS	F	P
Vehicle size	*	26051.4	13025.7	199.12	0.000
Type of silencer	*	1056.3	1056.3	16.15	0.000
Interaction	*	804.2	402.1	*	*
Error	*	1962.5	65.4		
Total	35	29874.3			

- c) Draw a response plot with the appropriate means in the table below. Does it suggest that there is interaction between Vehicle size and Type of silencer?

Table of means

Type of silencer	Standard	Vehicle size			All
		Small	Medium	Large	
		825.83	845.83	775.00	815.55
Type of silencer	Ectel filter	822.50	821.67	770.00	804.72
	All	824.17	833.75	772.50	810.14

- d) Using the F-value for interaction you calculated in b) above for the second table, carry out a significance test to determine whether there is any evidence of interaction between Vehicle size and Type of silencer.
- e) Calculate a suitable Least Significant Difference to compare the means for interaction in the table of means above. Explain which differences are significant and draw appropriate conclusions.

Bird feathers could serve as indicators of environmental pollution. Birds could be exposed to contaminants by direct contact or via ingestion of water or food. Raptors (birds of prey) are particularly good bioindicators because they feed at the top of the food chain and could accumulate contaminants to a level that is easily detectable. Table 10.1 below contains the concentration of cadmium (Cd), lead (Pb) and mercury (Hg) in falcon feathers (ppm dry weight) in three different regions of the country. The feathers of four different birds were used to measure metal concentrations for each region.

Metal concentrations (ppm dry weight) in feathers of falcons collected in three different regions of the country; Cd – cadmium, Pb – lead, Hg - mercury

		Region					
		1		2		3	
Heavy metal	Cd	0.62	0.58	0.58	0.61	0.61	0.60
		0.61	0.59	0.60	0.59	0.72	0.73
	Hg	0.62	0.58	1.53	1.71	3.16	2.96
		0.61	0.59	1.48	1.77	3.14	3.18
	Pb	1.18	1.21	2.76	2.45	0.93	0.87
		1.19	1.23	2.63	2.68	1.10	0.94

- a) The data in the table above are based on a factorial design with two factors. State the response variable, the factors, the levels for each factor, the number of replications for each treatment combination and the total number of observations.
- b) Use the MINITAB output in the table below to test for any evidence of:
- an interaction between the factors;
 - a main effect of either factor.

ANOVA for metal concentrations (ppm dry weight) in falcon feathers

Source	DF	SS	MS	F	P
Heavy metal	2	20.1604	10.0802	993.22	0.000
Region	2	0.1277	0.0638	6.29	0.006
Heavy metal*Region	4	10.9989	2.7497	270.93	0.000
Error	27	0.2740	0.0101		
Total	35	31.5610			

- c) Draw a response plot with the appropriate means from the table below. Does it suggest that there is interaction between Region and Heavy metal? [Tip: Put Heavy metal on the x-axis.]

Table of means

		Region			Overall Mean
		1	2	3	
Heavy metal	Cd	0.600	0.595	0.665	0.620
	Hg	2.622	1.623	3.110	2.452
	Pb	1.202	2.630	0.960	1.597
Overall Mean		1.475	1.616	1.578	1.556

- d) On the basis of your answers to (b) above calculate the LSD where appropriate and explain clearly what is shown by the study about the pollution by the three metals (Cd, Hg and Pb) in the three different regions of the country.

A nutritionist studied the inactivation of vitamin A in rancid fat (Sokal, RR & Rohlf FJ 1995. Biometry. New York: WH Freeman and Co.). As part of the study, the consumption of food by rats when it contained fresh or rancid fat was investigated. The experiment was carried out on 6 male and 6 female rats. Three randomly selected individuals from each sex were fed with food containing fresh fat and the other three individuals from each sex were fed food with rancid fat. Food consumption in grams was recorded. The data are presented in the table below.

Data on consumption of food (g) containing fresh or rancid fat by male and female rats

Rows: Sex		Columns: Type of Fat			
		Fresh		Rancid	
Male		709	679	699	592 538 476
Female		657	594	677	508 505 539

The data were analysed using analysis of variance. The computer output of this analysis is in the tables below. Some of the numbers have been replaced by asterisks.

Analysis of Variance for food consumption (g) by rats

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Type of Fat	*	61204	61204	61204	*	*
Sex	*	3781	3781	3781	*	*
Type of Fat*Sex	*	919	919	919	0.63	0.450
Error	*	11667	11667	1458		
Total	11	77570				

Treatment means for food consumption (g)

Rows: Sex		Columns: Type of Fat		
		Fresh	Rancid	All
Female		642.7	*	*
Male		*	535.3	615.5
All		669.2	*	597.8

- Give the name of the experimental design used in the above study? What are the two factors? What is the number of levels for each factor? How many are the treatment combinations? What is the number of replicates for each treatment? What is the total number of observations?
- In Analysis of Variance table above replace the asterisks in the columns with the appropriate values for the degrees of freedom and the appropriate F-values.
- Calculate the missing means in the Treatment Means table above and draw a response plot. What does the response plot suggest?
- Using the ANOVA output in the Analysis of Variance table above, including the missing F-values calculated in b) above, carry out significance tests to determine whether there is any effect of Fat Type, Sex or the interaction between the two on the amount of food consumed by a rat. Use the p-value if it is available and critical values otherwise.
- Is it appropriate to calculate a Least Significant Difference (LSD) for any of the sources of variation to test for differences among the respective treatment means in Table 10.3 above? Justify your answer.

In his paper (Quinn GP (1988) Ecology of the intertidal pulmonate limpet *Siphonaria diemenensis* Quoy et Garmard. II Reproductive patterns and energetics. *Journal of Experimental Marine Biology and Ecology* 117:137-156), the author investigated the effects of adult density and season on egg mass production by intertidal limpets. Quinn manipulated adult density by making enclosures with 6, 12 or 24 individuals. Studies were carried out during two seasons: spring and summer along the lower shoreline. The data are presented in the table below.

Data on limpet egg mass (g) by season and adult density

Rows: SEASON		Columns: DENSITY		
		6	12	24
spring		1.167	1.500	0.667
		0.500	0.833	0.667
		1.667	1.000	0.750
summer		4.000	3.330	2.540
		3.830	2.580	1.830
		3.830	2.750	1.630

The data were analysed using analysis of variance. The computer output of this analysis is in the table below. Some of the numbers have been replaced by asterisks.

- What is the name of the experimental design used by Quinn in the above study? What are the two factors? What is the number of levels for each factor? How many are the treatment combinations? What is the number of replicates for each treatment combination? What is the total number of observations?
- In the ANOVA table below replace the asterisks in the columns with the appropriate values for the degrees of freedom (DF), the mean square (MS) and the F-statistic, using the same precision as for the available values in the respective column.

Analysis of variance for limpet egg mass (g)

Source	DF	SS	MS	F	P
DENSITY	2	4.0019	*	13.98	*
SEASON	*	17.1483	17.1483	119.85	0.000
DENSITY*SEASON	*	1.6907	0.8454	*	0.016
Error	*	1.7170	0.1431		
Total	17	24.5580			

Treatment Means for limpet egg mass (g)

Rows: SEASON		Columns: DENSITY			
		6	12	24	All
spring		1.111	1.111	0.695	0.972
summer		3.887	2.887	2.000	2.924
All		2.499	1.999	1.347	1.948

- c) Use the means in Treatment Means table above to draw a response plot. What evidence for interaction between season and density does the response plot provide?
- d) Using the output in the ANOVA table above, including the missing F-statistic calculated in b) above, carry out hypotheses tests for any effect of Density, Season or the interaction between the two on limpet egg mass. Use the p-value if it is available and critical values for F otherwise.
- e) Calculate any appropriate Least Significant Difference (LSD) to test for differences among the appropriate means in the Treatment Means table above. Summarise your results in a couple of sentences.

9

A sociology student interested in our TV watching habits carried out a survey for his final year project. His data on the duration of TV watching per week (h) in relation to age group and gender is presented in the table below.

Duration of TV watching per week (h) by age group and gender; F: female, M: male; age group intervals are given in years

Rows: Gender		Columns: Age Group		
		20-25	26-55	56+
F		25	32	44
		21	26	45
		27	33	50
		26	33	43
		31	28	51
M		20	23	33
		27	21	34
		20	24	38
		22	28	33
		28	26	37

- a) Use the table above to answer the following questions. What experimental design did the student use in his study? What are the two factors involved? How many levels does each factor have? What is the number of treatment combinations? How many replicates did the student use for each treatment combination? What is the total number of observations he collected?

The data were analysed using analysis of variance. The computer output of this analysis is in the table immediately below. One p-value has been replaced by an asterisk.

Analysis of variance (ANOVA) for TV watching per week (h)

Source	DF	SS	MS	F	P
Age Group	2	1486.87	743.43	69.48	0.000
Gender	1	340.03	340.03	31.78	0.000
Age Group*Gender	2	103.27	51.63	4.83	*
Error	24	256.80	10.70		
Total	29	2186.97			

Treatment Means for duration of TV watching per week (h)

Rows: Gender		Columns: Age Group			
		20-25	26-55	56+	All
F		26.00	30.40	46.60	34.33
M		23.40	24.40	35.00	27.60
All		24.70	27.40	40.80	30.97

- Use the means in the Treatment Means table above to draw a response plot. What evidence for interaction between Gender and Age Group does the response plot provide?
- Using the output in the ANOVA table above, draw conclusions from hypothesis tests for any effect of Age Group, Gender, and the interaction between the two on the duration of TV watching per week (h). Use the p-value if it is available and critical values for F otherwise.
- Calculate any appropriate Least Significant Difference (LSD) to test for differences among the appropriate means in the Treatment Means table above. Summarize your results in a couple of sentences.

Headache sufferers are frequently sensitive to noise even when not suffering headache. One hypothesis put forward was that learning to relax might make a subject able to tolerate louder noise but that this might not be effective for all types of headache sufferer. Two groups of 22 subjects were chosen. One group comprised people suffering from migraine headaches (MH). The other group comprised people suffering from tension headaches (TH). Half of each group (11 subjects) were picked at random and were given relaxation training (RT). The other half received no treatment (NT). Each subject then listened to a tone gradually increasing in volume. The level of volume at which the subject found the tone unpleasant was recorded as score.

Raw data on score in relation to type of headache and type of treatment

Rows: headache Columns: treatment

	RT	NT
MH	5.70	2.80
	5.63	2.20
	4.83	1.20
	3.40	1.20
	7.20	0.43
	1.40	1.78
	4.03	3.50
	6.94	0.64
	6.88	0.95
	2.00	0.58
	1.56	0.83
TH	2.70	2.10
	4.65	1.42
	5.25	4.98
	3.78	3.36
	3.13	2.44
	3.27	3.20
	5.54	1.71
	5.12	1.24
	2.31	1.24
	1.36	2.00
	1.11	4.01

Cell Contents: score

- Describe the experimental design.
- Use the MINITAB output in the ANOVA table below to test whether there is evidence of interaction between headache type and treatment.
- Use the MINITAB output in the ANOVA table to complete the table of means below.

Table of means for score

		Treatment type		Overall Mean
		RT	NT	
Headache type	MH			
	TH			
	Overall Mean			

- d) Draw the response plot for the interaction between headache type and treatment.
- e) Calculate the appropriate LSD for comparing the means for interaction.
- f) Explain what conclusions could be drawn about the hypothesis put forward on the basis of the results from the study.

Analysis of variance (ANOVA) for score

```
MTB > ANOVA 'score' = 'headache' 'treatment' 'headache'*'treatment';
SUBC> Means 'headache' 'treatment' 'headache'*'treatment'.
```

Analysis of Variance for score

Source	DF	SS	MS	F	P
headache	1	0.001	0.001	0.00	0.982
treatment	1	43.960	43.960	18.24	0.000
headache*treatment	1	11.960	11.960	4.96	0.032
Error	40	96.390	2.410		
Total	43	152.312			

Means

headache	N	score
MH	22	2.9855
TH	22	2.9964

treatment	N	score
RT	22	3.9905
NT	22	1.9914

headache	treatment	N	score
MH	RT	11	4.5064
MH	NR	11	1.4645
TH	RT	11	3.4745
TH	NT	11	2.5182