

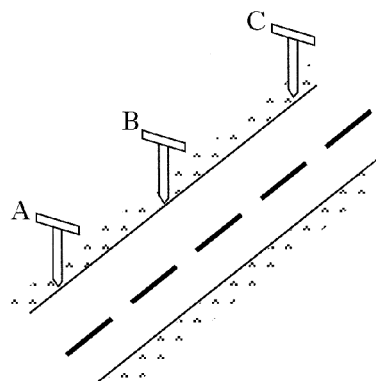
**ALL questions should be attempted.**

*Marks*

1. Find the equation of the straight line which is parallel to the line with equation  $2x + 3y = 5$  and which passes through the point  $(2, -1)$ . 3

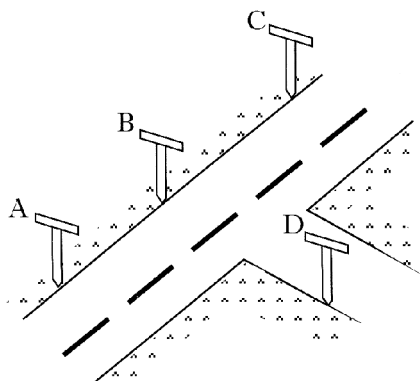
2. For what value of  $k$  does the equation  $x^2 - 5x + (k + 6) = 0$  have equal roots? 3

3. (a) Roadmakers look along the tops of a set of T-rods to ensure that straight sections of road are being created. Relative to suitable axes the top left corners of the T-rods are the points  $A(-8, -10, -2)$ ,  $B(-2, -1, 1)$  and  $C(6, 11, 5)$ . Determine whether or not the section of road ABC has been built in a straight line.



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- (b) A further T-rod is placed such that D has coordinates  $(1, -4, 4)$ . Show that DB is perpendicular to AB.



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4. Given  $f(x) = x^2 + 2x - 8$ , express  $f(x)$  in the form  $(x + a)^2 - b$ . 2

[Turn over]

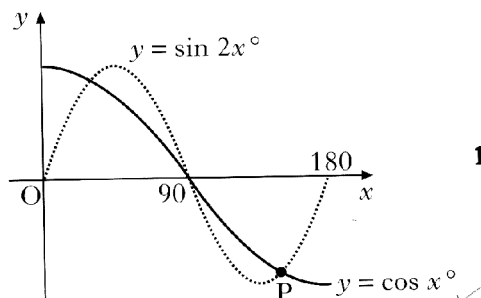
Marks

5. (a) Solve the equation  $\sin 2x^\circ - \cos x^\circ = 0$  in the interval  $0 \leq x \leq 180$ .

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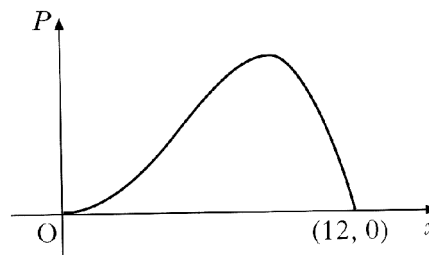
- (b) The diagram shows parts of two trigonometric graphs,  $y = \sin 2x^\circ$  and  $y = \cos x^\circ$ .

Use your solutions in (a) to write down the coordinates of the point P.



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6. A company spends  $x$  thousand pounds a year on advertising and this results in a profit of  $P$  thousand pounds. A mathematical model, illustrated in the diagram, suggests that  $P$  and  $x$  are related by  $P = 12x^3 - x^4$  for  $0 \leq x \leq 12$ . Find the value of  $x$  which gives the maximum profit.



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7. Functions  $f(x) = \sin x$ ,  $g(x) = \cos x$  and  $h(x) = x + \frac{\pi}{4}$  are defined on a suitable set of real numbers.

(a) Find expressions for:

- (i)  $f(h(x))$ ;  
(ii)  $g(h(x))$ .

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- (b) (i) Show that  $f(h(x)) = \frac{1}{\sqrt{2}} \sin x + \frac{1}{\sqrt{2}} \cos x$ .

- (ii) Find a similar expression for  $g(h(x))$  and hence solve the equation  $f(h(x)) - g(h(x)) = 1$  for  $0 \leq x \leq 2\pi$ .

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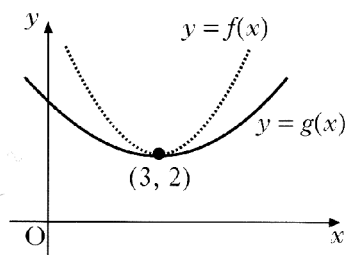
8. Find  $x$  if  $4 \log_x 6 - 2 \log_x 4 = 1$ .

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Marks

9. The diagram shows the graphs of two quadratic functions  $y = f(x)$  and  $y = g(x)$ . Both graphs have a minimum turning point at  $(3, 2)$ .

Sketch the graph of  $y = f'(x)$  and on the same diagram sketch the graph of  $y = g'(x)$ .

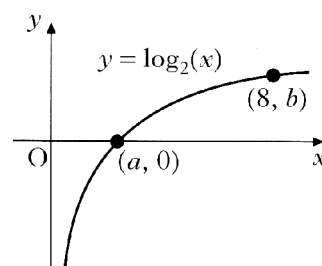


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10. The diagram shows a sketch of part of the graph of  $y = \log_2(x)$ .

(a) State the values of  $a$  and  $b$ .

(b) Sketch the graph of  $y = \log_2(x + 1) - 3$ .



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11. Circle P has equation  $x^2 + y^2 - 8x - 10y + 9 = 0$ . Circle Q has centre  $(-2, -1)$  and radius  $2\sqrt{2}$ .

(a) (i) Show that the radius of circle P is  $4\sqrt{2}$ .

(ii) Hence show that circles P and Q touch.

(b) Find the equation of the tangent to circle Q at the point  $(-4, 1)$ .

(c) The tangent in (b) intersects circle P in two points. Find the  $x$ -coordinates of the points of intersection, expressing your answers in the form  $a \pm b\sqrt{3}$ .

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[END OF QUESTION PAPER]